COLLABORATIVE FILTERING BASED ON CONTENT ADDRESSING

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Abstract: Collaborative Filtering (*CF*) is one of the most popular recommendation techniques. It is based on the assumption that users with similar tastes prefer similar items. One of the major drawbacks of the CF is its limited scalability, as the complexity of the CF grows linearly both with the number of available users and items. This work proposes a new fast variant of the CF employed over multi-dimensional content-addressable space. Our approach heuristically decreases the computational effort required by the CF algorithm by limiting the search process only to potentially similar users. Experimental results demonstrate that our approach is capable of generate recommendations with high levels of accuracy, while significantly improving performance in comparison with the traditional implementation of the CF.

1 INTRODUCTION

The quantity of available information grows rapidly and exceeds our cognitive processing capabilities. Thus, there is a pressing need for intelligent systems providing services tailored to users' real needs and interests. Recommender Systems (*RSs*) (Resnick & Varian, 1997) are one of the commonly used approaches to address this problem. These systems assist users to select a suitable item among a set of potential selectable items through applying statistical and knowledge discovery techniques (Sarwar et al, 2000). RSs are used in different domains, such as, movies (Good et al, 1999), jokes (Goldberg et al, 2001), music (Aguzolli et al, 2002), and many others.

Collaborative Filtering (CF) (Herlocker et al, 1999) is probably one of the most familiar and most widely-used techniques generate to recommendations in RSs. It relies on the assumption that people who agreed in the past will also agree in the future (Shardanand & Maes, 1995). The input for the CF algorithm is a matrix of users' ratings on a set of items, where each row represents ratings of a single user and each column represents ratings on a single item. CF aggregates the ratings to recognize similarities between users and generates new recommendation for an item by weighting the ratings of similar users on the item.

CF algorithm is typically partitioned to three generic stages: (1) Similarity Computation: weighting all the users with respect to their similarity with the active user (i.e., the user whose ratings are predicted), (2) Neighborhood Formation: selecting the most similar users for the prediction generation, and (3) Prediction Generation: computing the prediction by weighting the ratings of the selected users.

A major drawback of CF is its limited scalability. The stages of Similarity Computation and Neighborhood Formation require comparing an active user with all the other users over all the available ratings. Hence, the complexity of the CF grows both with the number of users and items in the ratings matrix. For a matrix containing ratings of M users on N items, computational complexity of the above stages is O(MN). This poses a problem in real-life systems, where the recommendations are generated using millions of ratings on thousands of items, e.g., Web-based RSs. Although previous studies, such as (Breese et al, 1998), (Goldberg et al, 2001), and (Chee et al, 2001) tackle the issue of reducing the computational effort required by the CF, it remains one of the most important issues in CF research.

In this work we develop a fast heuristic variant of the CF algorithm that decreases the computational effort required by the Similarity Computation and the Neighborhood Formation stages. The basic conjecture of the heuristic algorithm is that losing general completeness of the exhaustive search (1) has a minor negative effect on the accuracy of the predictions, but (2) significantly decreases the required computational effort. Thus, it provides a scalable approach, applicable to real-life scenarios with high number of users and items.

The proposed heuristic approach is based on a notion of content-addressable data management (Ratnasamy et al, 2001), providing an adaptive topology for mapping of users' profiles to a multidimensional space. This mapping implicitly clusters similar users and limits the Similarity Computation and the Neighborhood Formation stages to a heuristic search among highly similar users only.

Experimental evaluation of the proposed approach demonstrates high efficiency and good accuracy of the proposed algorithm, in comparison with the traditional (exhaustive) KNN search. The algorithm is also highly scalable with the number of nearest neighbors to be found.

The rest of the paper is organized as follows. Section 2 surveys the works focusing on the CF and the required computational effort reduction. Section 3 describes CAN, Peer-to-Peer content-addressable platform for decentralized data management. Section 4 describes the decentralized storage of users' profiles over CAN platform and elaborates on the proposed variant of the CF over CAN. Section 5 presents and analyzes the experimental results. Finally, section 6 lists our conclusions and presents a list of open questions for future research.

2 COLLABORATIVE FILTERING

Collaborative Filtering (*CF*) is probably one of the most familiar and widely-used recommendation techniques. An input for the CF is so-called *ratings matrix*, where each user is represented by a set of ratings given on various items, and each item is represented by a set of ratings given by the users.

CF requires similarity metric between users to be explicitly defined. The state-of-the-art CF systems exploit three similarity metrics: Cosine Similarity 0, Mean Squared Difference (MSD) (Pennock et al, 2000), and Pearson correlation (Sarwar et al, 2000). This work focuses on the MSD, computing the degree of similarity between users x and y by:

$$sim_{x,y} = \frac{\sum_{i=1}^{|x \cap y|} (R_{x,i} - R_{y,i})^2}{|x \cap y|}$$
(1)

where $|x \cap y|$ denotes the number of items rated by both users, and $R_{x,i}$ denotes the rating of user x on item *i*. In some sense, $sim_{x,y}$ can be considered as the *dissimilarity* of the users, as the lower the result of the MSD computation, the greater is the real similarity of the users.

Prediction $P_{a,j}$ for the rating of the user *a* on item *j* is computed as a weighted average of the ratings of his *K* most similar users, i.e., *K* nearest neighbors, by:

$$P_{a,j} = R_{a}' + \frac{\sum_{k=1}^{K} (R_{k,j} - R_{k}') \cdot sim_{a,k}}{\sum_{k=1}^{K} |sim_{a,k}|}$$
(2)

where $R_{x,y}$ denotes the rating of user x on item i, R_z' denotes the average rating of user z, and $sim_{v,u}$ denotes the level of similarity between users v and u.

The Similarity Computation stage of the CF requires comparing the active user with every other user in the system. For a ratings matrix storing the ratings of M users on N items, the computational complexity of the Similarity Computation stage is O(MN). This points on the poor scalability of the Similarity Computation stage, as the complexity grows linearly with both the number of users and the number of items in the matrix.

2.1 Reducing the Computational Effort Required by the CF

Many works deal with decreasing the computational effort required by the CF. In general, it is achieved either by preprocessing the ratings matrix, or by distributing the computationally intensive stages of the CF among multiple machines.

Various preprocessing techniques for decreasing the computational effort required by the CF (e.g., correlation coefficients, vector-based similarity, and statistical Bayesian methods) are discussed and analyzed in (Breese et al, 1998). Another technique, exploiting pre-clustering of the ratings matrix, is discussed in (Goldberg et al, 2001). There, principal component analysis is used to find two discriminative dimensions of the ratings matrix and all the vectors are projected onto the resulting plane. This inherently partitions the users to clusters or neighborhoods, which are further used to generate the recommendations. In (Chee et al, 2001), the authors use a tree-like data structure and apply a divide-and-conquer approach using an iterative Kmeans clustering to group the users. This leads to smaller and more homogeneous clustering of users for the recommendations generation stage.

An alternative approach is to distribute the CF and the required computational effort among the users, such that every user independently computes its similarity with the active user. This is initially proposed in (Tveit, 2001) and elaborated in (Sarwar et al, 2001). The latter also develops a detailed taxonomy of the CF distribution approaches and presents implementation frameworks for different application domains. PocketLens project (Miller et al, 2004) compares five decentralized distributed architectures for the CF. The experiments show that performance of the decentralized mechanism is similar to the performance of the centralized CF, while it provides increased robustness and security.

Further improvements to the decentralized CF are discussed in (Han et al, 2004) that proposes Peer-to-Peer platform for decentralized management of user profiles. However, it approximates the identification of the most similar users, and therefore, the accuracy of the prediction is reduced.

This work loosely bases on the ideas of CAN (Ratnasamy et al, 2001), content-addressable Peerto-Peer platform. We implement a fast heuristic variant of the CF, using CAN-like multi-dimensional space for maintaining connectivity of similar users. This allows to significantly decrease the computational effort required by the Similarity Computation and Neighborhood Formation stages through limiting the search process to a search among highly similar users only.

3 CONTENT-ADDRESSABLE DATA MANAGEMENT

This section present the general architecture of CAN (Ratnasamy et al, 2001), scalable decentralized data management platform. In CAN, the users are represented by nodes in virtual *N*-dimensional coordinate space. Each node maintains an *N*-dimensional subspace, called a *zone*. For example, consider a 2-dimensional space partitioned to 3 zones, maintained by the users *A*, *B*, and *C* (figure 1-left).

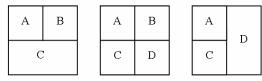


Figure 1: 2-Dimensional	l CAN	Space.
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Two nodes are called neighbors if their coordinate spans overlap along *N-1* dimensions and

adjoin along one dimension (e.g., nodes A and B in figure 1-left). To maintain connectivity, each node maintains a table of pointers to its neighbors. CAN's routing algorithm greedily forwards messages to the nodes that are closer to the target node than the current node (the distance metric exploited is the discrepancy in the address space). Thus, the messages are routed between any pair of CAN nodes in a logarithmic number of hops.

Also, CAN provides connectivity maintenance algorithm, stable to sporadic joins and departures of nodes. When a new node is inserted, it must be given its own zone. This is done by splitting a zone of one of the existing neighbors according to the following steps: (1) the new node finds an existing networks node, (2) the new node is routed to the target zone that will be split, and (3) the target zone is split and the neighbors of the new zone are updated to maintain connectivity and facilitate routings. Note, that only a subset of neighbors of the zone that was split is affected by the insertion of a new node.

The issue of splitting the target zone (i.e., how to split the existing zone, where the new node was mapped to) is one of the important issues affecting the performance of CAN. A number of policies are proposed, analyzed and compared in (Ratnasamy et al, 2001). The simplest policy for the zones splitting is so-called *ordered* splitting. According to this policy, the number of dimension across which a zone is split, iteratively increases from I to N.

For example, consider a node D joining CAN space (figure 1-middle). Assuming that the zone of a node C will be split, D is routed to C, and the zone is split across the horizontal dimension (i.e., the next split of the zones C or D will be performed across the vertical dimension and so forth). Finally, D notifies its neighbors, i.e., the nodes B and C, about the new node and the neighbors' pointers are updated. Note that in this case, only the zone that was split (C), and part of its neighbors (only B) are affected by the join of a node D, whereas other nodes are not affected.

Disconnections of nodes are handled in a similar manner. Disconnecting node finds a neighbor node that will take the responsibility for its zone, and updates other neighbors about the departure. For example, consider node B disconnecting (figure 1-right), and assume node D taking the responsibility for the zone previously managed by B.

Thus, CAN provides a decentralized platform, supporting (1) dynamic space partitioning and zones allocation, (2) efficient routing algorithm, and (3) connectivity maintenance algorithm over virtual *N*-

dimensional coordinate space. Note that distributed structure of CAN is not robust against sudden departures of node, as fault-tolerance is not one of the main goals of the platform. However, CAN facilitates completely decentralized self-manageable platform for content-addressable data management in distributed environment.

4 CF OVER CONTENT-ADDRESABLE SPACE

This work proposes a fast heuristic variant of the CF algorithm. It uses content addressing architecture for the purposes of optimizing traditional exhaustive search to a search among highly similar users only. Although our algorithm is heuristic by nature, experimental results demonstrate that it facilitates efficient search process without hampering the accuracy of the generated recommendations.

4.1 Mapping User Profiles

The input for the CF algorithm is a matrix of users' ratings on items, where each row (vector) represents the ratings of a single user and each column represents the ratings on a single item. The total number of items (N) defines an *N*-dimensional space, where the coordinates range in each dimension corresponds the range of ratings on the respective item.

To handle the ratings matrix in contentaddressable manner, we map it to CAN-like space. Each rating is projected using uniform *injective mapping* onto the appropriate dimension, such that the whole vector of length N is mapped to a single point in N-dimensional space. Thus, every user is represented in the space by a single node (whose location corresponds the set of ratings given by the user), and the respective zone (storing a list of neighbor zones). Users (through their ratings vectors) can be dynamically inserted and removed, since connectivity maintenance algorithm guarantees that the structure remains connected regardless of joins and disconnections of the nodes.

Deciding on the zones split policy affects the evolving structure of the ratings vectors. In our implementation, we used the above mentioned ordered splitting policy. This policy may be suboptimal in terms of the number of neighbor zones, resulting in less efficient algorithm, i.e., more comparisons or finding less similar neighbors. However, our experimental results indicate that the use of this simple policy considerably increases the efficiency of KNN, in comparison with traditional exhaustive search. Evaluating other splitting policies is beyond the scope of this work.

In addition to the guaranteed connectivity, content-addressable space *inherently clusters* similar users. Thus, the distance between two similar users (in our case, according to the MSD similarity metric) is lower than the distance between two arbitrary users. This is achieved through the use of injective mapping, preserving users' similarity while inserting the ratings vectors into the content-addressable space. The next subsection shows a use of the inherent clustering for the purpose of developing fast heuristic variant of the CF algorithm.

4.2 Heuristic Neighbors Search

The Neighborhood Formation stage of the CF over the evolving *N*-dimensional space can be schematically described as heuristically expanding breadth-first search. The algorithm for finding *K* Nearest Neighbors (KNN) of a user *x* is briefly explained by the following pseudo-code. It uses two lists of size *K*: (1) *CANDIDATES* – list of candidates for nearest neighbors, and (2) *KNN* – list of real nearest neighbors. In principle, the algorithm needs the *CANDIDATES* list only, as the *KNN* list is completely static. For the sake of clarity, we show an algorithm that uses two lists.

K_Nearest_Neighbors (user x)

- let KNN and CANDIDATES be lists of size K, initially empty
- (2) map(x) into the CAN space
- (3) foreach $u \in map(x) \bigcup neighbors(map(x))$
- (4) compute distance(x,u)
- (5) insert u into CANDIDATES, s.t. CANDIDATES is sorted by distances
- (6) for *i=1* to *K*
- (7) choose v from CANDIDATES, s.t. distance(x,v) is smallest
- (8) for each w in *neighbors*(v) s.t.
- distance(x,w) is not computed yet
 (9) compute distance(x,w)
- (10) insert w into CANDIDATES, s.t.
- it remains sorted by distances
- (11) move v from CANDIDATES to KNN
- (12) return KNN

Initially, the algorithm pretends to map the active user x to its location in the *N*-dimensional space (step 2). Next, the algorithm identifies the zone x is mapped to, and its neighbors, i.e., users managing the neighbor zones (step 3). For each of these zones,

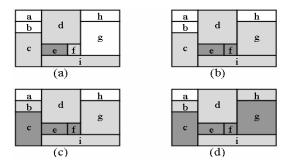
the degree of similarity, i.e., the distance between x and the relevant node, is computed. The neighbor node is inserted into the *CANDIDATES* list such that the candidate nodes are sorted according to their distances from the active user x (steps 4 and 5).

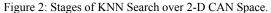
Then the algorithm iteratively performs the following operations:

- Selects v, the nearest neighbor stored in the *CANDIDATES* list (step 7),
- Identifies the neighbors of v that are not in the CANDIDATES list yet, computes their distances from x, and inserts them to the CANDIDATES, while keeping the list sorted (steps 8, 9, and 10).
- Removes *v* from the *CANDIDATES* list and inserts it to the *KNN* list.

Finally, the algorithm returns the resulting *KNN* list (step 12).

Consider an example execution of the *KNN* search as illustrated in figure 2. The initial structure of 2-dimensional space is depicted in figure 2a. Assume that the active user is mapped to the zone *e*.





Thus, e and its neighbors, i.e., nodes managing the zones c, d, f, and i, are the first candidates for the being nearest neighbors and they are added to the CANDIDATES list. Assume that the node managing the zone *e* is the closest one. It is moved from the CANDIDATES list to the KNN list (figure 2a). Since all the neighbors of e are already known, the next closest neighbor is chosen among its neighbors. Assume that the next closest neighbor is the node managing the zone f. It is moved from the CANDIDATES list to the KNN list, and its only new neighbor, node managing g, is added to the CANDIDATES list (figure 2b). The next closest neighbor is from the zone c, adding the node managing the zone b to the CANDIDATES list (figure 2c). Assume that the next closest neighbor is the node managing g (not a neighbor of e). It adds the node managing the zone h to the CANDIDATES list (figure 2d). This process is iteratively repeated until the KNN list contains K nearest neighbors.

The proposed algorithm reduces the computational effort required by the Similarity Computation and the Neighborhood Formation stages, in comparison with the traditional CF algorithm, where an active user is compared with all the available users. Conversely, the proposed heuristic algorithm compares the active users with potentially similar users only.

Since every user in the *N*-dimensional space continuously maintains an updated list of neighbors, any neighbor of a given user can be accessed through a single network hop. This is true regardless of the distance between the neighbors. Thus, the algorithm will also work in sparse spaces, where the distance between neighbors in the underlying network might be very high.

5 EXPERIMENTAL RESULTS

In the experimental part of our work we used Jester dataset of jokes (Goldberg et al, 2001). Jester is Web-based jokes RS, containing 4.1 millions of ratings (from -10.00 to +10.00) of 73,421 users on 100 jokes. We chose a subset of 14,192 users that rated all 100 jokes to get a dense matrix of *complete vectors* where every value corresponds to actual rating. We implemented a centralized simulation of a 100-dimensional space (space dimension equals to the number of rated jokes) and inserted the above 14,192 users into the space. Insertions of the users were done using the ordered splitting policy.

5.1 Scalability

These experiments were designed to evaluate the scalability of the proposed variant of KNN. The efficiency of CAN-based KNN is measured by the number of comparisons performed during the Neighborhood Formation stage of the CF.

In the first experiment we measured number of comparisons performed during the search. We gradually increased the number of users (*M*) in the system from M=1,000 to M=14,000. For each *M*, we computed the number of comparisons performed in the traditional exhaustive KNN search and in CAN-based variant of KNN. Both searches aimed to find K=5 nearest neighbors. For each value of *M*, the experiments were repeated 1,000 times for different active users. The results are shown on Figure 3.

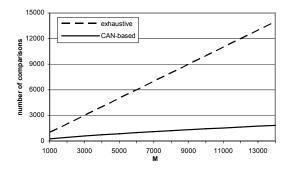


Figure 3: Average Number of Comparisons vs. M.

As expected, the number of comparisons in CAN-based KNN is significantly lower than in traditional KNN and it grows at a logarithmic-like manner with the number of users. This is explained by the fact that in CAN-based KNN the active user is compared only with a subset of highly similar users (located in a close vicinity in contentaddressable space), whereas in traditional KNN it is exhaustively compared with all other users.

To achieve a better understanding of comparison-based scalability of the proposed approach, we computed the ratio between the number of comparisons in CAN-based KNN and the number of comparisons in traditional (exhaustive) KNN. This ratio was computed for different values of M. The results show that the ratio steadily decreases with M. This allows us to conclude that the proposed algorithm is applicable in large-scale systems with high number of users and items, e.g., on the Web.

The second experiment evaluated the scalability of CAN-based KNN with the number of nearest neighbors (K) to be found. We gradually increased the value of K from K=1 to K=50. For each value of K, we measured the number of comparisons needed to find K nearest neighbors for M=1,000, 2,000,4,000, 8,000, and 14,000 users. For each value of M and K, the experiments were repeated 1,000 times for different active users. The number of comparisons as a function of K for the above values of M is shown on figure 4.

As can be clearly seen, the number of comparisons in CAN-based KNN remains roughly unchanged when *K* increases. This is explained by the observation that most of the KNN users are located in a close vicinity to the active user (this characterizes a real-life naturally clustered data). Thus, the similar users are discovered in the early stages of the KNN search, while further expansions contribute very few new similar users.

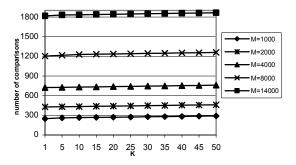


Figure 4: Average Number of Comparisons vs. K.

Both experiments show good scalability of CANbased KNN with *K*. This means, that practical RSs can use higher values of *K*, form a larger and more reliable neighborhood, and generate more accurate predictions with only a very minor computational overhead.

5.2 Accuracy

The following experiments were designed to evaluate the accuracy of the results obtained by the proposed heuristic variant of KNN. In the first experiment we compared the sets of users, i.e., the neighborhoods, found by the traditional (exhaustive) KNN and by CAN-based variant of KNN.

Let us denote by KNN_e the set of users found by the traditional exhaustive KNN search and by KNN_h the set of users found by CAN-based heuristic variant of KNN. Since CAN-based KNN is a heuristic approach, a sub-optimal structure of zones may lead to $KNN_e \neq KNN_h$. As predictions are produced by aggregating the ratings of similar users, identifying the most similar user is critical for producing an accurate prediction. Thus, we define the accuracy of CAN-based search by:

$$accuracy = \frac{|KNN_e \cap KNN_h|}{|KNN_h|}$$
(3)

The cardinality of the KNN_e set was K=10, while the cardinality of the KNN_h set was gradually increased from K'=1 to K'=100. The accuracy was computed for M=1,000, 2,000, 4,000, 8,000 and 14,000 users. For each value of M and K', the experiments were repeated 1,000 times for different active users. Figure 5 shows the accuracy as a function of K' for the above values of M.

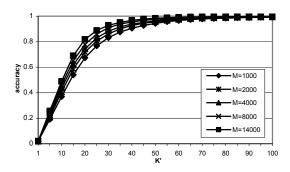


Figure 5: Precision of CAN-based KNN.

As can be clearly seen, the curves behave similarly and the accuracy increases with K', such that for K'>50 it is over 0.9 for all the given values of M. Previous experiments show that the algorithm is highly scalable with K. Thus, retrieving a larger set of users (i.e., higher values of K') leads to a minor increase in the computational overhead. Hence, it is reasonable to increase the number of neighbors found by CAN-based search in order to achieve higher accuracy and to generate better recommendations.

We evaluated the quality of the neighborhood found by CAN-based search by computing the average similarity between the nearest neighbors and the active user. This was compared to the average similarity of neighborhood found in an exhaustive manner. In addition, we evaluated the accuracy of the recommendations through well-known Mean Average Error (MAE) metric (Herlocker et al, 1999):

$$MAE = \frac{\sum_{i=1}^{N} |p_i - r_i|}{N}$$
(4).

where N denotes the number of predicted items, and p_i is the predicted, and r_i is the real rating on item *i*.

We gradually increased the number of users from M=1,000 to M=14,000. For each value of M, we compared the average similarity of heuristically found neighbors with the average similarity of exhaustively found neighbors for K=K'=10. We also generated the recommendations basing on both heuristically and exhaustively found neighborhoods. For each value of M, the above experiments were repeated 1,000 times for different active users. The results of the average similarity comparison are shown on figure 6, while MAE computation results are shown on figure 7.

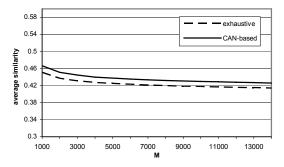


Figure 6: Average Similarity vs. M.

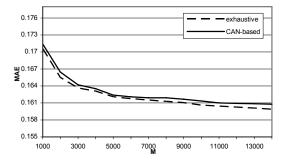


Figure 7: MAE of the Recommendations vs. M.

Although both the similarity and MAE of CANbased search are higher (i.e., the neighbors are more dissimilar and the accuracy is lower), the curves are very close and the results are quite similar. Average deviation of the similarities is 2.93% and of the MAEs is only 0.38%. This allows us to conclude that the proposed heuristic algorithm succeeds in producing both accurate neighborhoods and recommendations.

6 CONCLUSIONS AND FUTURE RESEARCH

One of the major drawbacks of the state-of-the-art CF implementations is their high computational complexity, which grows linearly both with the number of users and items in the system. In this work we propose to heuristically decrease the required computational effort through implementing the CF over content-addressable CAN-like *N*-dimensional space.

Experiments conducted over Jester dataset of jokes ratings show that proposed heuristic algorithm outperforms traditional exhaustive KNN search. Our algorithm decreases the number of required comparisons, while the ratio between the numbers of comparisons steadily decreases with the number of users. For example, for 14,000 users the number of comparisons was decreased by almost an order of magnitude (by 87%). Other experiment shows that the number of comparisons roughly remains unchanged when K increases. This allows us to increase the number of nearest neighbors to be retrieved (and to improve the accuracy of the prediction) with a very minor computational overhead.

In the accuracy experiments we compare the neighborhoods and the predictions found by CANbased KNN and by the traditional KNN. The found neighborhoods are similar and the recommendations are very close, which indicates on a high accuracy of the proposed algorithm. In summary, comparing the proposed heuristic KNN search with traditional exhaustive search shows that our algorithm achieves high accuracy (similar to the accuracy of the traditional exhaustive search), while significantly decreasing the required computational effort.

In this work, we assumed that user's ratings on all the items are available. Thus, the mapping of the ratings vectors to CAN space is straightforward. However, this is unachievable in many real-life scenarios, where an average user rates only a small portion of the available items. In the future, we plan to study CAN-based management of incomplete vectors, where part of the ratings is missing. Using statistical methods to complete the vectors through predicting the missing ratings might be a promising research direction.

In addition to decreasing the computational effort, our algorithm can naturally be extended to distribute it among multiple users. In traditional implementations of the CF, the Similarity Computation and the Neighborhood Formation stages are performed in a single central location. However, as the underlying CAN platform is originally distributed Peer-to-Peer platform, it inherently allows distributed and fully decentralized storage of the ratings matrix. In future, we plan to implement a distributed variant of the algorithm and to investigate the distribution issues.

The current work is limited to the Mean Squared Difference similarity metric, since the injective mapping to a multi-dimensional CAN-like space inherently supports it. However, for other metrics, such as Cosine Similarity or Pearson correlation, CAN space might be inappropriate and new types of topologies and the respective mappings should be developed. We plan to study other metrics and to produce a general framework for efficient heuristic Collaborative Filtering.

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